



Z හි පටු කෝණය සොයා ගැනීම සඳහා අපි සලකා බැලිය යුතුය.



$$Z = 1 - 2 \cos 60^\circ \cdot \cos 60^\circ + 1/2 \cos 60^\circ \sin 60^\circ$$

$$= 1 - 2 \cdot \frac{1}{2} \cdot \frac{1}{2} + 1 \cdot \frac{1}{2} \cdot \frac{\sqrt{3}}{2}$$

$$= \frac{1}{2} + \frac{\sqrt{3}}{2}$$

$$\frac{5-1}{2-3} = \frac{(5-1)(2-3)}{(2-3)(2-3)}$$

$$= \frac{10 + 15 - 2 - 3}{13} = \frac{13 + 13}{13}$$

$$= 1 + 1 = 2 \quad \therefore \lambda(1) = 0 \quad \text{එනම් } \lambda = 1$$

$$\left(\frac{5-1}{2-3}\right)^3 = (1+1)^3$$

$$= (1+1)^3$$

$$= (2)^3 \quad (\because 1^3 = -1)$$

$$= 8 \quad \therefore \lambda^3 = -8 \quad \text{එනම් } \lambda = -2$$

04. (ii) $x = 1 - \sin t \quad y = 1 - \cos t$

$$\frac{dy}{dt} = 1 - \cos t, \quad \frac{dx}{dt} = \sin t$$

$$\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx} = \sin t \cdot \frac{1}{1 - \cos t}$$

$$= \frac{2 \sin t/2 \cos t/2}{2 \sin^2 t/2}$$

$$= \cot t/2 \quad (\because \sin t/2 \neq 0)$$

$$\frac{d^2y}{dx^2} = \frac{d}{dx} \left(\frac{dy}{dx} \right)$$

$$= \frac{d}{dt} \left(\frac{dy}{dx} \right) \cdot \frac{dt}{dx}$$

$$= -\frac{1}{2} \operatorname{cosec}^2 t/2 \times \frac{1}{1 - \cos t}$$

$$= -\frac{1}{2} \operatorname{cosec}^2 t/2 \times \frac{1}{2 \sin^2 t/2}$$

$$= -\frac{1}{4} \operatorname{cosec}^4 t/2$$

$$\frac{d^3y}{dx^3} = \frac{d}{dt} \left(\frac{d^2y}{dx^2} \right) \cdot \frac{dt}{dx}$$

$$= -\frac{1}{4} \times 4 \operatorname{cosec}^3 t/2$$

$$\left[\operatorname{cosec} t/2 \cot t/2 \cdot \frac{1}{2} \right] \cdot \frac{1}{1 - \cos t}$$

$$= -\frac{1}{2} \operatorname{cosec}^4 t/2 \cot t/2 \cdot \frac{1}{2 \sin^2 t/2}$$

$$= \left[-\frac{1}{4} \operatorname{cosec}^4 t/2 \right] \cot t/2 \cdot \frac{1}{\sin^2 t/2}$$

$$\frac{d^3y}{dx^3} = -\left(\frac{d^2y}{dx^2} \right) \left(\frac{dy}{dx} \right) \cdot \frac{1}{1 - \cos t}$$

$$\frac{d^3y}{dx^3} = \left(\frac{d^2y}{dx^2} \right) \left(\frac{dy}{dx} \right)^2$$

$$= \left(\frac{d^2y}{dx^2} \right)^2 \left(\frac{dy}{dx} \right) = 0$$

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$$= \frac{4x^2 - (x^2 + 36)}{\sqrt{x^2 + 36} (2x + \sqrt{x^2 + 36})}$$

$$= \frac{3x^2 - 36}{\sqrt{x^2 + 36} (2x + \sqrt{x^2 + 36})}$$

$$= \frac{3(x - 2\sqrt{3})(x + 2\sqrt{3})}{\sqrt{x^2 + 36} (2x + \sqrt{x^2 + 36})}$$

$$\frac{dy}{dx} = 0, (x - 2\sqrt{3})(x + 2\sqrt{3}) = 0 \quad \therefore$$

$$\text{එනම් } x = 2\sqrt{3} \quad \text{හෝ } x = -2\sqrt{3}$$

$$\frac{dy}{dx} < 0, 0 < x < 2\sqrt{3} \quad \therefore$$

$$\frac{dy}{dx} = 0, x = 2\sqrt{3} \quad \therefore$$

$$\frac{dy}{dx} > 0, 2\sqrt{3} < x < 16$$

$$\text{එනම් } 0 < x < 2\sqrt{3} \quad \therefore \text{ අගය}$$

$$2\sqrt{3} < x < 16 \quad \therefore \text{ අගය}$$

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$$x = 2\sqrt{3} \quad \therefore \text{ අගය}$$

$$= \frac{1}{4} (1 + \sqrt{3}) = \frac{1}{4} (\sqrt{3} + 1)$$

$$\int x \ln x \, dx$$

$$= \int \ln x \cdot \frac{d}{dx} \left(\frac{x^2}{2} \right) dx$$

$$= \left[\ln x \cdot \frac{x^2}{2} \right]_2^4 - \int_2^4 \frac{x^2}{2} \cdot \frac{1}{x} dx$$

$$= \left[\frac{x^2}{2} \ln x \right]_2^4 - \frac{1}{2} \left[\frac{x^2}{2} \right]_2^4$$

$$= \frac{16}{2} \ln 4 - \frac{1}{2} \ln 2 - \frac{1}{2} \left(\frac{16}{2} - \frac{4}{2} \right)$$

$$= 8 \ln 4 - 2 \ln 2 - \frac{1}{2} \times \frac{12}{2}$$

$$= 2 \ln 4^4 - \ln 2 - 3$$

$$= 2 \ln 256 - 3$$

$$= 2 \ln 128 - 3$$

$$\text{එනම් } \frac{7x - x^2}{(2-x)(x^2+1)} = \frac{A}{2-x} + \frac{Bx+C}{x^2+1}$$

$$\text{එනම් } 7x - x^2 = A(x^2+1) + (Bx+C)(2-x)$$

$$x = 2 \Rightarrow 14 - 4 = 5A \Rightarrow A = 2$$

$$x^2 = 0 \Rightarrow 0 = 2A + 2C \Rightarrow C = -2$$

$$1 = A - B \Rightarrow B = 3$$

$$\text{එනම් } \frac{7x - x^2}{(2-x)(x^2+1)} = \frac{2}{2-x} + \frac{3x-2}{x^2+1}$$

$$\int \frac{7x - x^2}{(2-x)(x^2+1)} dx = \int \frac{2}{2-x} dx + \int \frac{3x-2}{x^2+1} dx$$

$$= -2 \ln |2-x| + \int \frac{3x-2}{x^2+1} dx$$

$$= -2 \ln |2-x| + \int \frac{3x}{x^2+1} dx - \int \frac{2}{x^2+1} dx$$

$$= -2 \ln |2-x| + \frac{3}{2} \ln |x^2+1| - \int \frac{2}{x^2+1} dx$$

$$= -2 \ln |2-x| + \frac{3}{2} \ln |x^2+1| - 2 \arctan x$$

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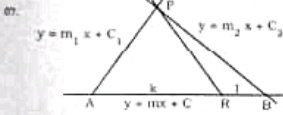
$$= -2 \ln |2-x| + \frac{3}{2} \ln |x^2+1| - 2 \arctan x$$

$$= -2 \ln |2-x| + \frac{3}{2} \ln |x^2+1| - 2 \arctan x$$

$$= -2 \left[\ln 1 \cdot \ln 2 \right] + \frac{3}{2} \left[\ln(x^2 + 1) \right]_0^1$$

$$= 2 \ln 2 - \frac{3}{2} \left[\ln 2 - \ln 1 \right] - \tan^{-1} 1 = 0$$

$$= \frac{2}{2} \ln 2 - \frac{3}{2} \ln 2 + \frac{3}{2} = \frac{3}{2} - \frac{\ln 2}{2}$$



$A = (x_1, y_1)$ සහ $B = (x_2, y_2)$ ලෙස ගනිමු.

$A \Rightarrow B \quad y = mx + C$ සමීකරණය.

$y_1 = mx_1 + C \Rightarrow y_1 - y_2 = m(x_1 - x_2)$

$y_2 = mx_2 + C$

$A, y = mx + C$ සමීකරණය.

$y_1 = mx_1 + C \Rightarrow y_1 - y_2 = m(x_1 - x_2)$

$B, y = mx + C$ සමීකරණය.

$y_2 = mx_2 + C \Rightarrow y_2 - y_1 = m(x_2 - x_1)$

එබැවින් $R = \left[\frac{kx_2 + y_1}{k+1} - \frac{ky_2 + y_1}{k+1} \right] = 0$

PR හි සමීකරණය $u_1 + \lambda u_2 = 0$ ලෙස ගනිමු.

එබැවින් $(y_1 - y_2) \cdot C_1 + \lambda (y_2 - y_1) \cdot C_2 = 0$

එබැවින් R ලෙස ගනිමු.

$\left[\frac{kx_2 + y_1}{k+1} - m_1 \left(\frac{kx_2 + y_1}{k+1} \right) \cdot C_1 \right]$

$+ \lambda \left[\frac{ky_2 + y_1}{k+1} - m_2 \left(\frac{kx_2 + y_1}{k+1} \right) \cdot C_2 \right] = 0$

$\Rightarrow (ky_2 + y_1) \cdot m_1 (kx_2 + y_1) \cdot C_1 (k+1)$

$+ \lambda [(ky_2 + y_1) \cdot m_2 (kx_2 + y_1) \cdot C_2 (k+1)] = 0$

$(y_1 - m_1 x_1) \cdot C_1 + \lambda (y_2 - m_2 x_2) \cdot C_2 = 0$

$+ \lambda [(y_1 - m_1 x_1) \cdot C_1 + (y_2 - m_2 x_2) \cdot C_2] = 0$

$+ \lambda [(y_1 - m_1 x_1) \cdot C_1 + (y_2 - m_2 x_2) \cdot C_2] = 0$

(පිටු 0 හි 0 ලෙස)

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$\Rightarrow k[y_2 \cdot m_1 x_2 - (y_1 \cdot m_1 x_1)]$

$+ \lambda [y_1 \cdot m_2 x_1 - (y_2 \cdot m_2 x_2)] = 0$

$\Rightarrow k[y_2 - y_1 \cdot m_1 (x_2 - x_1)]$

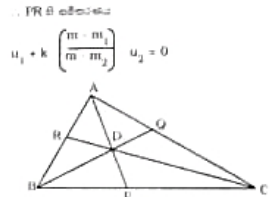
$+ \lambda [y_1 - y_2 \cdot m_2 (x_1 - x_2)] = 0$

$\Rightarrow k \left[\frac{y_1 - y_2}{x_1 - x_2} + m_1 \right]$

$+ \lambda \left[\frac{y_1 - y_2}{x_1 - x_2} - m_2 \right] = 0$

$\Rightarrow k(m_1 + m_2) + \lambda(m_1 - m_2) = 0$

$\lambda = k \frac{(m_1 - m_2)}{(m_1 + m_2)}$



$u_{AB} = y - \frac{3}{2}x - 3 = 0$

$u_{BC} = y - 2x - 2 = 0$

එනම් $u_{AC} = y + x - 3 = 0$

$m_{AB} = -3/2, m_{BC} = -2, m_{AC} = -1$

(ii) 0 හි 0 ලෙස $\frac{1}{2}x = 0 \Rightarrow x = 0$

එබැවින් $y = 3$

$A = (0, 3)$

(iii) CR හි සමීකරණය

$u_{CA} = k \left(\frac{m_{AB} - m_{BC}}{m_{AB} - m_{AC}} \right) u_{BC} = 0$

එබැවින් $k = \frac{1}{2}, AR = \frac{1}{2} RB$ ලෙස ගනිමු.

එබැවින් $x + y - 3 + \frac{1}{2} \left[\frac{3}{2} + 1 \right] (2x + y - 2) = 0$

ප්‍රශ්න විචල්‍ය

$\Rightarrow x + y - 3 + \frac{1}{2}(-1)(2x + y - 2) = 0$

$x + y - 3 - x/2 + y/2 + 1 = 0$

$\Rightarrow y - 4 = 0$ එනම් CR හි සමීකරණය.

BQ හි සමීකරණය

$u_{AB} + k \left(\frac{m_{AC} - m_{AB}}{m_{CA} - m_{BC}} \right) u_{BC} = 0$

එබැවින් $k = 2/3$ ($\therefore AQ = \frac{2}{3} QC$)

එබැවින් $\frac{3}{2}x + y - 3 + \frac{2}{3} \left[\frac{1 + 3/2}{-1 - 2} \right] (2x + y - 2) = 0$

එබැවින් $\frac{3}{2}x + y - 3 + \frac{2}{3} \left[\frac{1}{-3} \right] (2x + y - 2) = 0$

$9x + 6y - 18 + 2(2x + y - 2) = 0$

$13x + 8y - 22 = 0$

$PB^2 = \frac{16}{49} + \frac{64}{49} = \frac{80}{49} \Rightarrow PB = \frac{\sqrt{80}}{7}$

$AP : PB = \sqrt{289} : \sqrt{80}$

18. දී ඇති රේඛාවල සමීකරණ (x_1, y_1) සහ (x_2, y_2) සඳහා සමීකරණ $(x_1, y_1) = (x_2, y_2)$ ලෙස ගනිමු.

එබැවින් (x_1, y_1) හි සමීකරණය $u_{AB} + k \left(\frac{m_{AC} - m_{AB}}{m_{CA} - m_{BC}} \right) u_{BC} = 0$

එබැවින් $k = 2/3$ ($\therefore AQ = \frac{2}{3} QC$)

එබැවින් $\frac{3}{2}x + y - 3 + \frac{2}{3} \left[\frac{1 + 3/2}{-1 - 2} \right] (2x + y - 2) = 0$

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$9x + 6y - 18 + 2(2x + y - 2) = 0$

$13x + 8y - 22 = 0$

$u_{AB} + k \left(\frac{m_{AC} - m_{AB}}{m_{CA} - m_{BC}} \right) u_{BC} = 0$

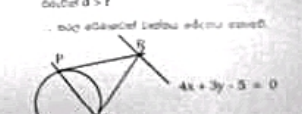
එබැවින් $k = 2/3$ ($\therefore AQ = \frac{2}{3} QC$)

එබැවින් $\frac{3}{2}x + y - 3 + \frac{2}{3} \left[\frac{1 + 3/2}{-1 - 2} \right] (2x + y - 2) = 0$

එබැවින් $\frac{3}{2}x + y - 3 + \frac{2}{3} \left[\frac{1}{-3} \right] (2x + y - 2) = 0$

$9x + 6y - 18 + 2(2x + y - 2) = 0$

$13x + 8y - 22 = 0$



ප්‍රශ්න විචල්‍ය

R හි P හි Q හි ස්වයංසන්ධිත වර්ගය සොයන්න.

$$R: 4x + 3y - 5 = 0 \text{ හි } A, B$$

$$R = \left[1, \frac{5-4t}{3} \right] \text{ ලෙස ගනිමු.}$$

එදින එදින වෙනස් වීමක් $ax + by + c = 0$ බව සලකමු. R හි ඇති ස්වයංසන්ධිත ස්වයංසන්ධිත වීමක්.

$$x(1 + y \left(\frac{5-4t}{3} \right)) + 1(x + y) + 3 \left(y + \frac{5-4t}{3} \right) + 1 = 0$$

$$3xt + y(5-4t) + 3(x+1) + 9y + 3(5-4t) + 3 = 0$$

$$x(3t+3) + y(14-4t) + (18-9t) = 0$$

එදින වෙනස් වීමක් සොයා බලමු.

$$\frac{3t+3}{a} = \frac{14-4t}{b} = \frac{18-9t}{c}$$

$$\text{එදින } a = \frac{3b(t+1)}{2(7-2t)} \text{ හි } c = \frac{9b(2-t)}{2(7-2t)}$$

එදින එදින එදින.

$$\frac{3b(t+1)}{2(7-2t)} x + by + \frac{9b(2-t)}{2(7-2t)} = 0$$

$$\text{එදින } 3b(t+1)x + 2b(7-2t)y + 9b(2-t) = 0$$

$$\Rightarrow 3(t+1)x + 2(7-2t)y + 9(2-t) = 0$$

$$\Rightarrow 3x + 14y + 18 + t(3x - 4y - 9) = 0$$

$$\text{එදින } 3x + 14y + 18 = 0 \text{ හි}$$

$3x - 4y - 9 = 0$ වන විට වෙනස් වීමක් සොයා බලමු.

එදින වෙනස් වීමක් සොයා බලමු.

A, B හි වෙනස් වීමක් සොයා බලමු.

18. (a) $\sin^3 2x \cos 6x + \cos^3 2x \sin 6x$

$$= \left[\frac{3 \sin 2x \cdot \sin 6x}{4} \right] \cos 6x + \left[\frac{\cos 6x + 3 \cos 2x}{4} \right] \sin 6x$$

$$= \frac{1}{4} (3 \sin 2x \cos 6x + \sin 6x \cos 6x + \cos 6x \sin 6x + 3 \cos 2x \sin 6x)$$

$$= \frac{3}{4} (\sin 2x \cos 6x + \cos 2x \sin 6x)$$

$$= \frac{3}{4} \sin (2x + 6x)$$

$$= \frac{3}{4} \sin 8x$$

$$\sin^3 2x \cos 6x + \cos^3 2x \sin 6x = a$$

$$\Rightarrow \frac{3}{4} \sin 8x = a \text{ හි } \sin 8x = \frac{4a}{3}$$

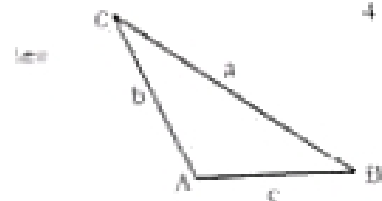
එදින වෙනස් වීමක් සොයා බලමු.

$$-1 \leq \sin 8x \leq 1 \text{ හි}$$

$$\text{එදින } -1 \leq \frac{4a}{3} \leq 1$$

A, B හි වෙනස් වීමක් සොයා බලමු.

$$\frac{3}{4} \leq a \leq \frac{3}{4} \text{ හි}$$



අනෙක් වෙනස් වීමක් සොයා බලමු.

$$A = 2C \text{ හි } a = \frac{3}{2} c \text{ හි}$$

ABC හි වෙනස් වීමක් සොයා බලමු.

$$\frac{\sin A}{a} = \frac{\sin C}{c}$$

$$\text{එදින } \frac{\sin 2C}{\frac{3}{2} c} = \frac{\sin C}{c}$$

$$\Rightarrow 2 \sin C \cos C = \frac{3}{2} \sin C$$

$$\sin C \neq 0 \text{ හි } 2 \cos C = \frac{3}{2}$$

$$\Rightarrow \cos C = \frac{3}{4} \text{ හි } C = \cos^{-1} \left(\frac{3}{4} \right)$$

$$A = 2C \Rightarrow B = \pi - 3C$$

$$\text{එදින } \frac{\sin B}{b} = \frac{\sin C}{c}$$

$$b = 10 \text{ cm හි}$$

$$\frac{\sin (\pi - 3C)}{10} = \frac{\sin C}{c} \Rightarrow \frac{\sin 3C}{10} = \frac{\sin C}{c}$$

එදින

$$\frac{3 \sin C - 4 \sin^3 C}{10} = \frac{\sin C}{c}$$

$$\Rightarrow \frac{\sin C (3 - 4 \sin^2 C)}{10} = \frac{\sin C}{c}$$

$$\Rightarrow 3 - 4(1 - \cos^2 C) = \frac{10}{c} (\sin C \neq 0)$$

$$\Rightarrow -1 + 4 \cos^2 C = \frac{10}{c} \Rightarrow -1 + 4 \cdot \frac{9}{16} = \frac{10}{c}$$

$$\Rightarrow \frac{5}{4} = \frac{10}{c} \Rightarrow c = 8 \text{ cm හි}$$

$$= \frac{3}{2} \times 8 = 12 \text{ cm හි}$$